Bulk Energy Dissipation Mechanism for the Fracture of Tough and Self-Healing Hydrogels

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Supporting Information

ABSTRACT: Recently, many tough and self-healing hydrogels have been developed based on physical bonds as reversible sacrificial bonds. As breaking and re-forming of physical bonds are time-dependent, these hydrogels are viscoelastic and the deformation rate and temperature profoundly influence their fracture behavior. Using a polyampholyte hydrogel as a model system, we observed that the time–temperature superposition principle is obeyed not only for the small strain rheology but also for the large strain hysteresis energy dissipation and the fracture energy below a certain temperature. The three processes possess the same shift factors that obey the equation of Williams, Landel, and Ferry (WLF) time–temperature equivalence. The fracture energy \( \Gamma \) scales with the crack velocity \( V_c \) over a wide velocity range as \( \Gamma \sim V_c^\alpha \) (\( \alpha = 0.21 \)). The exponent \( \alpha \) of the power law is well-related to the exponent \( \kappa \) of the relaxation modulus \( G(t) \sim t^{-\kappa} \) (\( \kappa = 0.26 \)), obeying the prediction \( \alpha = \kappa/(1 + \kappa) \) from classic viscoelasticity theory. These results show that the fracture energy of the polyampholyte gel is dominated by the bulk viscoelastic energy dissipated around the crack tip. This investigation gives an insight into designing tough and self-healing hydrogels and predicting their fracture behaviors from their dynamic mechanical spectrum.

1. INTRODUCTION

Over the past decade, various mechanically strong and tough hydrogels have been invented, which substantially broaden the possible uses of hydrogels in hygiene and medical fields, for example, as cell scaffolds, drug delivery agents, and load bearing structural biomaterials. The basic principle for developing tough hydrogels is to incorporate energy dissipation structures (sacrificial bonds) into the hydrogels. Generally, these tough gels can be classified into two categories depending on their molecular mechanisms to dissipate energy. One is elastic double network hydrogels. The energy dissipation of these hydrogels is by the breaking of sacrificial covalent bonds of the brittle network, which is independent of the observation time window in the conventional time scale. The other is viscoelastic supramolecular hydrogels. These hydrogels contain abundance physical bonds, and energy is dissipated by breaking these sacrificial physical bonds, which strongly depends on the observation time window. Nanocomposite hydrogels, such as those with clay or silica nanoparticles, also belong to the latter type whereupon the energy dissipation is believed to occur mainly at the polymer–inorganic composite interface. The viscoelastic tough hydrogels usually exhibit self-resilient and self-healing behaviors due to the reversible nature of physical bonds.

For the application as load-bearing materials, understanding the failure mechanism and predicting the failure behavior of these tough hydrogels are indispensable. In the case of the elastic double network hydrogels, it has been shown that the energy required to advance a crack is dissipated in the large damage zone formed in front of the crack tip, in which the brittle network is substantially damaged. Such a toughening mechanism has also been applied to double and triple network elastomer systems. In the case of viscoelastic supramolecular hydrogels, few are known. It is highly possible that the energy required to advance a fracture plane by one-unit area includes not only the energy necessary to break the polymer chains ahead of the crack tip but also the bulk viscoelastic energy dissipated around the crack tip, in similar to viscoelastic solids, such as rubbers.

The purpose of this work is to study the fracture behavior and its energy dissipation mechanism of tough supramolecular hydrogels with sacrificial physical bonds. As a model system, we use a polyampholyte (PA) physical hydrogel, which is strongly viscoelastic and exhibits excellent mechanical properties, such as high strength and extensibility, high fracture energy, self-

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resilience, and self-healing. The PA gel is synthesized from the radical copolymerization of cationic monomers and anionic monomers at a very high concentration with balanced charges. The polyampholytes thus obtained are topologically entangled, and each polymer chain possesses oppositely charged ionic groups randomly distributed along the chain backbone. By dialysis of small counterions and co-ions in pure water, ionic associations between opposite charges on the polymer chains, both intra- and interchains, are switched on, which gives microphase-separated PA hydrogels containing ∼50 wt % of water. In our previous paper, the PA hydrogels were described by a dichotomic molecular picture of the elastic network with weak bonds and strong bonds, where upon the weak bonds can break to dissipate energy and re-form to impart self-healing, and strong bonds can maintain the integrity of the physical hydrogel over much longer time scale. Given the microphase-separated structure and the wide integrity of the physical hydrogel over much longer time scale, PA gels, which is essentially different from double network hydrogels that contain only chemical cross-linkers.

The mechanical behaviors of the viscoelastic gels are strongly dependent on the relative relation of observation time and the physical bond lifetime. Furthermore, the lifetime of physical bonds depends not only on the bond association energy but also on the observation temperature, as the bond breaking probability is related to the ratio of bond energy to thermal energy. Thus, deformation rate and temperature pronouncedly influence the mechanical and fracture behavior of the physical PA gels, which is essentially different from double network hydrogels that contain only chemical cross-linkers.

In this work, three sets of experiments—the rheological test for small strain behavior, the cyclic tensile test for large strain behavior, and the tearing test for fracture behavior—were performed over a wide range of deformation rate and environmental temperature. The validity of Williams, Landel, and Ferry (WLF) time—temperature equivalence is discussed for the three sets of experimental results. The results are further analyzed using the classic viscoelasticity theory.

2. EXPERIMENTAL SECTION

Synthesis of Hydrogels. Tough PA hydrogels of stoichiometric charge composition were synthesized by the radical copolymerization of a cationic monomer 3-(methacroyloxypropyltrimethylammonium chloride (MPTC) and an anionic monomer p-styrene-sulfonate (NaSS) with a monomer ratio NaSS:MPTC = 0.525:0.475 at a total monomer concentration 2.1 M, as described in the previous work. A mixed aqueous monomer solution together with 0.25 mol % UV initiator, 2-oxoglutaric acid (relative to the total monomer concentration), was injected into a reaction cell consisting of a pair of glass plates with a 2 mm spacer, and the reaction cell was irradiated by UV light (∼365 nm) for 11 h. After polymerization, the as-prepared gel was immersed in a large amount of water for 1 week to reach the equilibrium and to wash away the residual chemicals.

Rheological Test. Dynamic rheological test was performed with an ARES rheometer (advanced rheometric expansion system, Rheometric Scientific Inc.). The disk-shaped sample with a diameter of 15.0 mm and a thickness of 1.3 mm was fixed between metal plates by using super glue (Konishi Co., Ltd.). In order to prevent water evaporating from the gel, the sample was surrounded by water during the measurement. Prior to each measurement, the autostrain function and manual gap adjustment were used to minimize compression on the sample. The rheological tests were performed over a wide range of frequency (0.1–100 rad/s) at different temperature environment (0.1–56 °C) at a shear strain of 0.1%. The temperature of water, controlled by a thermal bath, was increased stepwise from low to high. Before each measurement, the sample was held at the set temperature for 300 s to reach the equilibrium.

Cyclic Tensile Test. The sample for the cyclic tensile test was cut into a dumbbell shape with standard JIS-K6251-7 size (12.0 mm (gauge length) × 2.0 mm (width)). The sample thickness was 1.3 mm. The test was performed on a tensile-compressive tester (Tensilon RTC-1310A, Orientec Co.), and the sample was stretched to a large engineering strain (ε = 2) and unloaded to the original position with the same loading—unloading velocity in a water bath with different temperature (8, 24, 40, and 56 °C). The nominal stress σ was obtained from the tensile force divided by the initial cross-sectional area of the sample. The strain rate, ε, is defined as the ratio of stretch velocity to the gauge length (12.0 mm). Hysteresis or energy dissipation, $\Gamma_{hys}$, is calculated from the area enclosed by the loading—unloading curve. Three measurements were performed for each sample and results are mean of the three trials.

Tearing Test. To measure the tearing energy of PA gels, the mode III tearing test, known as the trousers test, was performed on a commercial test machine (Tensilon RTC-1310A, Orientec Co.). The sample was cut into a standard JIS-K6252 1/2 size (50.0 mm length × 7.5 mm width) with an initial notch length ∼20.0 mm. The two arms of the hydrogel were clamped tightly by metal plates to prevent the sample from slipping during the tearing test. To make sure the crack advanced along the central line through the entire sample, the two arms were set perpendicular to the object surface of the clamps. Then the lower clamp was stretched at a constant stretch velocity, and the crack propagated through the entire sample and by the corresponding tearing force $F$ and stretched displacement $L$ were recorded during the test. To directly relate the local deformation to tearing energy at the crack tip during crack propagation, the crack propagation velocity $V_c$ was recorded in situ by a digital camera. To control the temperature and prevent water evaporating from the samples, the tearing test was performed in a water bath at a described temperature (8, 24, 40, and 56 °C). The tearing energy $\Gamma$ was calculated using the relation

$$\Gamma = 2F/w$$

where $w$ is the thickness of the sample and $F$ is the constant tearing force at crack propagation. Three measurements were performed for each sample, and results are the mean of the three trials.

3. RESULTS AND DISCUSSION

The polyampholyte physical gel, containing 52 wt % water, is very tough. At a stretching strain rate of 0.14 s⁻¹, it shows a clear yielding around strain 0.5, a high fracture strength of 1.8 MPa, and a large fracture stain of 8. At an angular frequency of 62.8 rad/s, the hydrogel exhibits a softening temperature at 48.2 °C. These results are consistent with the previous report. Previous reports also show that this gel possesses weak bonds with a relaxation time $\tau_0 \sim 3$ s and strong bonds with a relaxation time longer than $\sim 10^4$ s and a characteristic creep time longer than $10^5$ s.

Time—Temperature Superposition at Small Strain. According to the linear rheological theory, the principle of time—temperature superposition (TTS) holds for viscoelastic solids, and it is possible to superimpose linear viscoelastic data taken at different temperature. The dynamic modulus at any given temperature, containing storage modulus $G'$ and loss modulus $G''$, can be superimposed on data at a reference temperature $T_0$ using a time scale multiplicative horizontal shift factor $\alpha_T$ and a modulus scale multiplicative vertical shift factor $b_T$.
Figure 1. Linear dynamic behavior of polyampholyte (PA) hydrogels. (a, b) Constructed master curves of storage modulus $G'$ and loss modulus $G''$ (a) and loss factor tan $\delta$ (b) following the principle of time—temperature superposition. (c, d) Time—temperature horizontal shift factor $a_T$ (c) and vertical shift factor $b_T$ (d) as a function of temperature. Reference temperature $T_0 = 24$ °C.

$$G'(t, T) = b_T G(t/a_T, T_0) \quad \text{and} \quad G''(t, T) = b_T G(t/a_T, T_0)$$

(2)

The $a_T$ and $b_T$ are treated as adjustable parameters, related to the temperature dependence of diffusion coefficient and variations in density, respectively. We first performed the linear viscoelastic test by frequency sweep at different temperatures (Figure S1). According to the TTS principle, we construct master curves of $G'$, $G''$, and tan $\delta$ for the polyampholyte hydrogel at a reference temperature of 24 °C. As shown in Figure 1a,b, master curves can be constructed very well over a wide frequency range of $10^{-5}$ to $10^5$ rad/s. To further check the validity of time—temperature superposition, phase angle $\delta$ versus the complex modulus $G^*$ is plotted in Figure S1. This way of plotting can yield the temperature-independent curves when time—temperature superposition holds. Results exhibit a smooth curve of $\delta$ vs $G^*$ curve in the range of performed temperature, indicating that the ionic bonds, regardless of their wide distribution in strength, have the same temperature dependence, and the physical PA gel shows this thermorheologically simple behavior.\(^{10,47}\) We also found that at high temperature (from 56 to 95 °C) the TTS does not hold, indicating that some structure changes occur at elevated temperature although the gel still looks opaque (data are not shown).

We further found that $a_T$ used to construct the master curves of dynamic behavior, well follows the Williams—Landel—Ferry (WLF) function\(^{38}$\)

$$\log a_T = -\frac{C_1(T - T_0)}{C_1 + (T - T_0)}$$

where $C_1 = 58.6$ and $C_2 = 504.2$ are two constants and $T_0$ is the reference temperature (= 24 °C) (Figure 1c). The $b_T$, introduced to account for the small changes in polymer density at different temperatures, is very close to 1, again confirming the thermorheologically simple behavior of this gel (Figure 1d).

The dynamic spectrum in Figure 1a shows that over the accessible frequency range, $\omega$, from $10^{-5}$ to $10^5$ rad/s, the PA sample increases its storage and loss moduli gradually with the frequency, and the storage modulus is always higher than the loss modulus. The storage modulus at high frequency is about 100 times that at low frequency. The mechanical spectrum shows a very broad tan $\delta$ peak around the frequency of $\omega_0 \approx 0.3$ rad/s, which gives a characteristic relaxation time of $\tau_0 = 1/\omega_0 \approx 3$ s (Figure 1b). These results are in good agreement with our previous report.\(^{10}$ The dynamic spectrum indicates that this PA gel has abundant ionic bonds with a characteristic relaxation time around the common time scale of interest, and these bonds are so-called weak bonds in our previous paper.\(^{10}$ When $1/\omega$ is comparable to $\tau_0$, most weak bonds break around this time scale, and the hydrogel exhibits the viscoelastic features. When $1/\omega \gg \tau_0$, most weak bonds are relaxed and the gel shows the soft rubbery response. It is noticed that even at a frequency of $10^{-5}$ rad/s, the sample still exhibits an elastic nature with a storage modulus ($\sim 10^5$ Pa) higher than the loss modulus, indicating that the longest relaxation time is far longer than $10^5$ s at 24 °C (Figure 1a). For $1/\omega \ll \tau_0$ there is no time for most of the weak bonds to break, and the hydrogel responses like in the glassy state with a high dynamic modulus ($> 2 \times 10^7$ Pa) and a small loss factor tan $\delta$. So the hydrogel is very stiff and approximately elastic (brittle-like).

**Time—Temperature Equivalence to Large Strain Energy Dissipation.** For some viscoelastic hydrogels, it has been shown that the amplitude of strain can be decoupled from the time dependency, resulting in modulus which decreases...
with the deformation time. Such decoupling is also approximately applicable for the current system. This fact suggests that the breakage of weak bonds is dominated by the thermal activation process whereupon the forced debonding effect does not play a substantial role. This motivates us to study the bulk energy dissipation at large strain and to correlate the data with the small strain behaviors obtained in Figure 1.

Figure 2a shows the cyclic tensile behaviors of the sample at a large fixed peak strain $\varepsilon = 2$, far above the yielding point. Large hysteresis is observed over the cyclic stress-strain curves, indicating the energy dissipation by the breaking of the weak bonds. It has been confirmed that in the strain range tested the sample is fully self-resilient and the hysteresis loop disappears after a certain waiting time. The area of hysteresis markedly increases with increasing cyclic stretch rate, indicating that more ionic bonds contribute to the energy dissipation at high strain rate. As shown in Figure 2b, we found that the relation between the hysteresis energy $U_{\text{hys}}$ and the cyclic strain rate $\dot{\varepsilon}$ follows a power law, $U_{\text{hys}} \sim \dot{\varepsilon}^m$, nicely at different temperatures. Raising the temperature expedites the bond breaking and therefore reduces the hysteresis energy of the hydrogel. The index $m$ varies in the range of $m = 0.26$–$0.43$ for the temperature performed but does not show a simple trend with temperature.

To investigate the correlation between the hysteresis data and the linear rheological data, we use the same shift factors $a_T$ and $b_T$ obtained from the linear rheology in Figure 1c,d to build a master curve of energy dissipation. We found that the hysteresis energy at the large strain can be reduced to a master curve with the strain rate, as shown in Figure 2c. This result means that the effect of temperature on the hysteresis can be accounted for simply by applying $a_T$ and $b_T$ to $\dot{\varepsilon}$ at a reference temperature $(T_0 = 24 \degree C)$:

$$U_{\text{hys}}(\dot{\varepsilon}, T) = b_T U_{\text{hys}}(a_T \dot{\varepsilon}, T_0)$$

(3)

This result demonstrates that hysteresis energy also follows the time-temperature superposition principle with the same shift factors as those for the small strain rheological observation. This means that the linear rheology is also applicable to the bulk energy dissipation at large deformation, and the bond breaking process is thermally activated and hardly depends on the applied strain. This is consistent with the strain-amplitude-time decoupling observed in tensile tests of the material. In the range of strain rate $10^{-5}$–$10^2$ s$^{-1}$, a scaling relationship is found as $U_{\text{hys}} \sim \dot{\varepsilon}^{0.31}$.

**Time-Temperature Equivalence to Tearing Energy.**

The tearing energy, $\Gamma$, namely the energy required to propagate a crack by a unit area, was measured by the tearing test, as shown in Figure 3a. The typical force-displacement curves $(F-L)$ obtained from the tearing test with different tearing velocities, $V_t$, at 24 $\degree C$ are presented in Figure 3b. At a given tearing velocity, the two legs of notched sample are elongated without advancing of the crack tip, and the force increases with elongation until reaching a plateau; then the crack propagation starts at the position shown by the arrows in the figure and soon reaches a constant velocity. With the increase of the tearing velocity, the force required to elongate the sample and to advance the crack increases, as the bond lifetime becomes relatively longer for a shorter observation time. To directly relate the tearing energy to local crack propagation process, the constant crack velocity, $V_c$, was estimated from a synchronized

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**Figure 2.** Cyclic tensile behavior of the polyampholyte (PA) hydrogel. (a) Cyclic stress–strain curves $(\sigma–\varepsilon)$ at 24 $\degree C$ under various cyclic stretch strain rate. (b) Relationship between hysteresis $U_{\text{hys}}$ and cyclic strain rate $\dot{\varepsilon}$ under various testing temperature. (c) The constructed master curve of hysteresis $U_{\text{hys}}$ against stretch strain rate $\dot{\varepsilon}$ using the same shift factors $a_T$ and $b_T$ determined from the linear rheology in Figures 1c and 1d, respectively. Reference temperature $T_0 = 24 \degree C$. 

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video. Except for the points at high tearing velocity, all the observed crack velocities at various temperatures are slightly lower than the applied tearing velocities over a wide range, as shown in Figure S2. We correlate the calculated tearing energy to the crack velocity under various temperatures, and the results are shown in Figure 3c. Raising the temperature expedites bond breaking and therefore reduces the tearing energy of the gel. Tearing energy increases with crack velocity, following power law relations \( \Gamma \sim V_c^\alpha \) nicely at different temperatures. The index of the power law, \( \alpha \), varies in the range of 0.18–0.28 for the temperature performed but does not show a simple trend with temperature.

It has been shown that for viscoelastic rubbers the energy required to advance a fracture plane by a unit area includes the intrinsic fracture energy of the polymer network ahead of the crack tip and the bulk viscoelastic energy dissipated around the crack tip.\(^{19-28}\) The tearing energy of rubber strongly depends on the crack velocity, and is greatly enhanced by viscous dissipative losses that are several orders of magnitude larger than the intrinsic fracture energy of the polymer network.\(^{23-25,27,28}\) The fracture energy of viscoelastic solids is usually described by the following equation: \( \Gamma(V_c,T) = \Gamma_s(1 + f(V_c,T)) \), where the viscoelastic dissipation term \( f(V_c,T) \) is related to crack velocity \( V_c \) and temperature \( T \), and \( \Gamma_s \) is a threshold value of the polymer network below which no fracture occurs.\(^{25,27,28,42,43}\) During crack propagation, the intrinsic fracture energy of a polymer network involves several complex processes, including chain breaking, cavitation formation, and so on, while the bulk viscoelastic energy dissipation only involves the viscoelastic deformation process around the crack tip. When the fracture energy is dominated by the viscoelastic energy dissipation, the fracture behavior is governed by the bulk viscoelasticity and the fracture properties may be correlated to viscoelastic data (Figure 2c). That is the effect of temperature on the fracture energy can be accounted for simply by applying shift factors \( a_T \) and \( b_T \) determined from the linear rheology in Figures 1c and 1d, respectively. Reference temperature \( T_0 = 24 \, ^\circ\mathrm{C} \). The arrows in the insets of (b) correspond to the positions that crack propagation starts.

Following this equivalence, we found that as shown in Figure 3d, all the tearing energy data measured at different temperatures and crack velocities can be reduced to a nice master curve at a reference temperature \( T_0 = 24 \, ^\circ\mathrm{C} \) when the same shift factors \( a_T \) and \( b_T \) determined from the linear dynamic measurement in Figures 1c and 1d are used, respectively. The result indicates that the equivalence holds for the PA hydrogel: \( \Gamma(V_c,T) = b_T\Gamma(a_TV_cT_0) \). Therefore, the tearing energy obtained for a higher velocity at a given temperature has the same value as that measured at the lower velocity and low temperature according to the time–temperature equivalence.\(^{27,28}\)

Figure 3. Fracture behavior of the polyampholyte (PA) hydrogel. (a) An image of the sample during a tearing test. (b) Force–displacement curves \( (F–L) \) of the tearing test at 24 °C at different tearing velocities. (c) Relationship between tearing energy \( \Gamma \) and crack velocity \( V_c \) at different testing temperature. (d) The constructed master curves of tearing energy \( \Gamma \) against crack velocity \( V_c \) using the same shift factors \( a_T \) and \( b_T \) determined from the linear rheology in Figures 1c and 1d, respectively. Reference temperature \( T_0 = 24 \, ^\circ\mathrm{C} \).
It is noticed that even at a crack velocity as low as $10^{-3}$ m/s (Figure 3d) the tearing energy still shows a velocity dependence. Furthermore, the tearing energy is $\sim 200$ J/m$^2$ at such low velocity. This tearing energy, regardless of the 50 wt % water content of the PA gel, is much larger than the usual threshold value of rubber materials ($\sim 50$ J/m$^2$) that do not contain any solvents.\(^{35}\) This indicates that even at such a low crack velocity, the bulk energy dissipation still dominates the tearing energy in PA gel. This is in consistent with the extremely long creep time of the system.\(^{31}\)

**Figure 4.** (a) The energy dissipative model for the fracture of viscoelastic solids. The energy dissipation profile at the crack tip consists of three different zones depending on the distance $r$ from the crack tip: the unrelaxed zone at the crack tip ($G_\infty$), viscoelastic energy dissipative zone around the crack tip ($G_{\text{vis}}$), and the fully relaxed zone that is far from the crack tip ($G_0$).\(^{31,22,25,28}\) (b) Circular birefringence images of the PA hydrogel undergoing crack growth at velocities, $1.7 \times 10^{-3}$ m/s (1), $1.7 \times 10^{-2}$ m/s (2), and $1.7 \times 10^{-1}$ m/s (3) during pure shear test. The images were taken at the strain $\varepsilon = 1.5$. The data are adopted from ref.\(^{32}\) (c) The relaxation modulus, $G(t)$, obtained from the dynamic modulus, $G(\omega)$, at various angular frequencies in Figure 1a.

Correlation between Relaxation Modulus and Fracture Energy. Here, we intend to correlate the dynamic mechanical spectrum with the crack velocity dependence of the fracture energy. For this purpose, let us first revisit the bulk energy dissipative model for the fracture of viscoelastic solid materials.\(^{21,25,27,28}\) The model assumes that the viscoelastic solid is described by a single relaxation time $\tau$, with two plateau moduli, $G_0$ and $G_\infty$, at low frequency ($\omega \tau \ll 1$) and high frequency ($\omega \tau \gg 1$), respectively. Given that the deformation rate at a distance $r$ from the crack tip is characterized by the angular frequency $\omega = V_c/r$, the energy dissipation profile at the crack tip consists of three different zones depending on the distance $r$ from the crack tip (Figure 4a).\(^{21,25,27,28}\) Near the crack tip, where $r$ is very small, the zone is in the hard glassy state with modulus $G_\infty$ as frequency $\omega$ becomes very high ($\omega \tau \gg 1$). Far from the crack tip with large $r$ ($\omega \tau \ll 1$), the zone is in the rubbery state with modulus $G_0$. At the intermediate distance $r$ ($\omega \tau \sim 1$), the zone is in the viscoelastic state, giving large energy dissipation. In our previous work on the PA gels, we indeed observed the above-described regions by pure shear test under circular polarized light (Figure 4b).\(^{32}\) Given a crack velocity $V_c \sim 1.7 \times 10^{-3}$ m/s at strain $\varepsilon = 1.5$ (Figure 4b(1)), the region near the crack tip was very stiff, and the crack advanced with a constant opening angle. Ahead of the crack tip, the region had a complicated stress field, and there was a large yielding zone with significant viscoelastic dissipation, as indicated by the butterfly shaped birefringence pattern. The region far away from the crack tip corresponded to the pure shear zone with a uniform birefringence color. With increasing crack advancing velocity, the crack opening angle decreased (Figure 4b(2,3)), indicating that the region near the crack tip became more rigid. The size of the yielding zone, where most viscoelastic dissipation took place, increased with the crack velocity (Figure 4b). In the framework of the bulk energy dissipation model, several theoretical works have discussed the crack velocity dependence of fracture energy and its correlation with the viscoelastic relaxation spectrum $G_\omega$ in the transition region.\(^{19,22,25,28}\) Several theories have tried to correlate the power-law relationship of fracture energy $\Gamma$ and crack velocity $V_c$, $\Gamma \sim V_c^\alpha$ to the linear viscoelastic response of bulk materials, using the creep compliance function by Schapery or stress relaxation function by Persson.\(^{19,27,28}\) For example, the theory predicts that the exponent $\alpha$ of $\Gamma \sim V_c^\alpha$ and the exponent $\kappa$ of $G(t) \sim t^\kappa$ by the power law relationship of the relaxation modulus $G(t)$ and time $t$ in the viscoelastic transition region, can be correlated as follows:

$$\alpha = \kappa/(1 + \kappa)$$

This theoretical relation has been verified by several experiments on rubbers.\(^{35,46}\) Here, we analyze our results using Persson’s theory. Before doing this, we should check whether the frequency range over which the viscoelastic spectrum was measured (Figure 1a, $\omega \tau = 10^{-5} - 10^5$ rad/s) covers the deformation frequency range in front of the crack tip during crack propagation. Given the lower limit of $r$ the size of monomer ($\sim 0.3$ nm) and the upper limit of the width of the sample arm ($\sim 3.8$ mm), we can estimate the deformation frequency range using the relation $\omega = V_c/r$ (Figure 3d). For $V_c = 10^{-8} - 10^{-6}$ m/s, the high angular frequency bound close to the crack tip is in the range $\omega = 3 \times 10^{-3} - 3 \times 10^5$ rad/s using $r = 0.3$ nm. Although our observed high frequency bound ($10^6$ rad/s) is much lower than $3 \times 10^5$ rad/s, and can only cover the range $r > 10 \mu m$ for the high velocity $V_c = 1$ m/s, the energy dissipation at the zone $r < 10 \mu m$ may not make dominant contribution to the tearing energy for two reasons: (1) the tan $\delta$ peak is around $\omega_0 = 0.3$ rad/s (Figure 1b), which corresponds to $r = 0.03 \mu m - 3.3$ m for the measured crack velocity range of $V_c = 10^{-8} - 10^{-6}$ m/s. This means, except at the low crack velocity limit, the viscoelastic region is located at a distance much larger than $r = 10 \mu m$. (2) As the dynamic properties only depend on the distance to the crack tip $r$, the energy dissipation in a zone with distance $r$ and width $dr$ is proportional to $\sim 2\pi r\, dr$. Accordingly, even at a relatively small crack velocity, the region close to the crack tip contributes less to the energy dissipation than that of the large $r$. This implies that bulk viscoelastic energy dissipation dominates the total fracture energy of samples under the observation time range. This is why the measured fracture energy ($\sim 200$ J/m$^2$) at the minimum crack
velocity $\sim 10^{-8}$ m/s is larger than the common value of the intrinsic fracture energy of polymer networks (Figure 3d).

To analyze our results using Persson’s theory, we transform the data of dynamic modulus $G'(\omega)$ and $G''(\omega)$ in Figure 1a into the relaxation modulus $G(t)$ based on the linear viscoelasticity theory through the intermediate relaxation time spectrum $H(\tau)$. All both the relaxation modulus and dynamic modulus can be calculated by superimposing Maxwell relaxation modes, and each relaxation mode has a characteristic relaxation time $\tau$:

$$G(t) = G'_0 + \int_{-\infty}^{+\infty} H(\ln \tau) e^{-\tau / \tau} \, d \ln \tau \quad (5)$$

$$G'(\omega) = \int_{-\infty}^{+\infty} H(\ln \tau) \frac{\omega^2 \tau^2}{1 + \omega^2 \tau^2} \, d \ln \tau \quad (6)$$

$$G''(\omega) = \int_{-\infty}^{+\infty} H(\ln \tau) \frac{\omega \tau}{1 + \omega^2 \tau^2} \, d \ln \tau \quad (7)$$

Here, $G'_0$ is the equilibrium modulus which is zero for physical PA gels. The continuous relaxation time spectrum $H(\tau)$, as shown in Figure S3, is calculated from the dynamic modulus $G'(\omega)$ and $G''(\omega)$ by using the built-in nonlinear regression procedures of the ARES rheometer. Then, $G(t)$ is obtained from $H(\tau)$, as shown in Figure 4c. By fitting the data with the power law relation $G(t) \sim t^{-\kappa}$ in the range of $10^{-5} - 10^5$, we obtained the exponent $\kappa = 0.26$. Substituting the $\kappa$ value into eq 4, one can predict that the exponent of the power law of the tearing energy and crack velocity, $\alpha$, is 0.21, $\Gamma \sim V_c^{0.21}$. This value obtained using the linear viscoelastic fracture theory is in excellent agreement with the experimental observation ($\Gamma \sim V_c^{0.21}$) (Figure 3d). The above results show that at this observation time scale the crack propagation energy indeed has the form $\Gamma(V_c,T) = \Gamma_0(1 + f(V_c,T))$ and is dominated by the viscoelastic energy term $f(V_c,T)$. The viscoelastic theory is able to predict the fracture data from the linear viscoelastic spectrum.

When comparing the experimental results with the theoretically predicted value, two remarks should be made. One is that a single relaxation mode at this range of stress relaxation function is considered in Figure 4c. Several relaxation modes can be observed from the curve of $G(t) \sim t^{-\kappa}$ in Figure 4c, which leads to oversimplification of the theoretical consideration. Another is the applicability of linear fracture mechanics in the region close to the crack tip. In the region that is far away from the crack tip, the self-healing behavior of the gel makes the breaking and healing of physical bonds independent of strain and strain rate at small values, and the rupture of bonds can be re-formed again with a shorter healing time than that of breaking time. The healed bonds do not carry load and cannot be stretched to large deformation. The fracture energy is dissipated by rupture of bonds and releasing the elastic energy of the chain. The applied linear fracture theory to this region is suitable. However, close to the crack tip the local deformation and deformation rates become very high, and polymer chains can be stretched to a very high level before breaking of the physical bonds (strain hardening). In such case the decoupling of amplitude of strain from the time dependency fails to hold for the current system, and the forced debonding effect may play a role, where the linear fracture mechanics may no longer apply, although the contribution to the fracture energy in this range is very low. How the local strain fields around the crack tip effect crack propagation behavior should be considered in future work.

4. CONCLUSIONS

Although the physical polyampholyte hydrogels show a phase-separated structure and a very broad relaxation spectrum, the dynamic modulus, the tensile hysteresis, and the tearing energy all follow the principle of time—temperature superposition. The tearing energy increases with observed crack velocity, as a power law relationship, $\Gamma \sim V_c^{0.21}$ and is correlated to the relaxation modulus $G(t) \sim t^{-0.26}$ by Persson’s viscoelastic theory. These results indicate that (1) the physical PA gel exhibits the thermorheologically simple behavior and all the ionic bonds, either strong or weak, have the same temperature dependence, (2) the tearing energy of the PA hydrogel is dominated by the bulk viscoelastic energy dissipation in front of the crack tip, and (3) linear viscoelastic theory is applicable for this supramolecular hydrogel system containing solvent, as like solid rubbers. The simple correlation between the dynamic spectrum of fracture energy and the relaxation modulus indicates that the dynamic mechanical spectrum can be used as a fingerprint for designing tough viscoelastic hydrogels.

■ ASSOCIATED CONTENT

9 Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.macromol.7b00162.

Figure S1: linear dynamic behavior of physical polyampholyte hydrogels; Figure S2: relationship between the crack velocity $V_c$ and tearing velocity $V_t$ at different temperatures; Figure S3: the relaxation time spectrum of the PA gel calculated from the data of dynamic modulus (PDF).

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Notes

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